

PhysicsByAaryan

CSIR NET · GATE · JEST · BARC – Physics

GATE Physics 2012 — Full Question Paper

Previous Year Questions with Official Answer Key

Inside this PDF

- Every GATE Physics (PH) 2012 question, in order
- Marking scheme + question type (MCQ/MSQ/NAT) on every question
- Subject & topic classification per question
- Official answer key at the end

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Questions
with answer key

*Questions taken from official GATE Physics (PH) papers conducted by IITs / IISc.
Compiled by PhysicsByAaryan for free use by aspirants. Answer key at the end of this PDF.*

Q1. [Marks: 1 | MCQ]

Mathematical Physics · Vector Analysis

GATE 2012	MCQ	1M
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Identify the CORRECT statement for the following vectors $\vec{a} = 3\hat{i} + 2\hat{j}$ and $\vec{b} = \hat{i} + 2\hat{j}$

- (A) The vectors \vec{a} and \vec{b} are linearly independent
- (B) The vectors \vec{a} and \vec{b} are linearly dependent
- (C) The vectors \vec{a} and \vec{b} are orthogonal
- (D) The vectors \vec{a} and \vec{b} are normalized

Q2. [Marks: 1 | MCQ]

Classical Mechanics · Rotation Motion

GATE 2012	MCQ	1M
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Two uniform thin rods of equal length, L , and masses M_1 and M_2 are joined together along the length. The moment of inertia of the combined rod of length $2L$ about an axis passing through the midpoint and perpendicular to the length of the rod is,

(A) $(M_1 + M_2) \frac{L^2}{12}$

(B) $(M_1 + M_2) \frac{L^2}{6}$

(C) $(M_1 + M_2) \frac{L^2}{3}$

(D) $(M_1 + M_2) \frac{L^2}{2}$

Q3. [Marks: 1 | MCQ]

Electromagnetism · EM Waves

GATE 2012	MCQ	1M
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The space-time dependence of the electric field of a linearly polarized light in free space is given by $x E_0 \cos(\omega t - kz)$ where E_0 , ω and k are the amplitude, the angular frequency and the wavevector, respectively. The time averaged energy density associated with the electric field is

- (A) $\frac{1}{4} \epsilon_0 E_0^2$
- (B) $\frac{1}{2} \epsilon_0 E_0^2$
- (C) $\epsilon_0 E_0^2$
- (D) $2 \epsilon_0 E_0^2$

Q4. [Marks: 1 | MCQ]

Electronics · Diodes

GATE 2012	MCQ	1M
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If the peak output voltage of a full wave rectifier is 10 V, its d.c. voltage is

- (A) 10.0 V
- (B) 7.07 V
- (C) 6.36 V
- (D) 3.18 V

Q5. [Marks: 1 | MCQ]

Quantum Mechanics · Potential Well

GATE 2012	MCQ	1M
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A particle of mass m is confined in a two dimensional square well potential of dimension a . This potential $V(x, y)$ is given by

$$V(x, y) = 0 \text{ for } -a < x < a \text{ and } -a < y < a \\ = \infty \text{ elsewhere}$$

The energy of the first excited state for this particle is given by,

- (A) $\frac{\pi^2 \hbar^2}{ma^2}$
- (B) $\frac{2\pi^2 \hbar^2}{ma^2}$
- (C) $\frac{5\pi^2 \hbar^2}{2ma^2}$
- (D) $\frac{4\pi^2 \hbar^2}{ma^2}$

Q6. [Marks: 1 | MCQ]

Thermodynamics · Laws of thermodynamics

GATE 2012	MCQ	1M
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The isothermal compressibility, κ of an ideal gas at temperature T_0 and volume V_0 , is given by

(A) $-\frac{1}{V_0} \frac{\partial V}{\partial P} \Big|_{T_0}$

(B) $\frac{1}{V_0} \frac{\partial V}{\partial P} \Big|_{T_0}$

(C) $-V_0 \frac{\partial P}{\partial V} \Big|_{T_0}$

(D) $V_0 \frac{\partial P}{\partial V} \Big|_{T_0}$

Q7. [Marks: 1 | MCQ]

Atomic and Molecular Physics · Effects in atomic physics

GATE 2012	MCQ	1M
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The ground state of sodium atom (^{11}Na) is a $^2S_{1/2}$ state. The difference in energy levels arising in the presence of a weak external magnetic field B , given in terms of Bohr magneton, μ_B , is

(A) $\mu_B B$

(B) $2\mu_B B$

(C) $4\mu_B B$

(D) $6\mu_B B$

Q8. [Marks: 1 | MCQ]

Solid State Physics · Free electron model

GATE 2012	MCQ	1M
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For an ideal Fermi gas in three dimensions, the electron velocity v_F at the Fermi surface is related to electron concentration n as,

- (A) $v_F \propto n^{2/3}$
- (B) $v_F \propto n$
- (C) $v_F \propto n^{1/2}$
- (D) $v_F \propto n^{1/3}$

Q9. [Marks: 1 | MCQ]

Nuclear and Particle Physics · Particle Physics

GATE 2012	MCQ	1M
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Which one of the following sets corresponds to fundamental particles?

- (A) proton, electron and neutron
- (B) proton, electron and photon
- (C) electron, photon and neutrino
- (D) quark, electron and meson

Q10. [Marks: 1 | MCQ]

Nuclear and Particle Physics · Particle detector and accelerator

GATE 2012	MCQ	1M
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In case of a Geiger-Muller (GM) counter, which one of the following statements is CORRECT?

- (A) Multiplication factor of the detector is of the order of 10^{10}
- (B) Type of the particles detected can be identified
- (C) Energy of the particles detected can be distinguished
- (D) Operating voltage of the detector is few tens of Volts

Q11. [Marks: 1 | MCQ]

Electromagnetism · EM Waves

GATE 2012	MCQ	1M
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A plane electromagnetic wave traveling in free space is incident normally on a glass plate of refractive index $3/2$. If there is no absorption by the glass, its reflectivity is

- (A) 4%
- (B) 16%
- (C) 20%
- (D) 50%

Q12. [Marks: 1 | MCQ]

Solid State Physics · Semiconductor Physics

GATE 2012	MCQ	1M
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A Ge semiconductor is doped with acceptor impurity concentration of 10^{15} atoms /cm³. For the given hole mobility of $1800 \text{ cm}^2/\text{V} - \text{s}$, the resistivity of this material is

- (A) $0.288\Omega \text{ cm}$
- (B) $0.694\Omega \text{ cm}$
- (C) $3.472\Omega \text{ cm}$
- (D) $6.944\Omega \text{ cm}$

Q13. [Marks: 1 | MCQ]

Thermodynamics · Kinetic theory of gases

GATE 2012	MCQ	1M
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A classical gas of molecules, each of mass m , is in thermal equilibrium at the absolute temperature, T . The velocity components of the molecules along the Cartesian axes are v_x , v_y and v_z . The mean value of $(v_x + v_y)^2$ is

- (A) $\frac{k_B T}{m}$
- (B) $\frac{3}{2} \frac{k_B T}{m}$
- (C) $\frac{1}{2} \frac{k_B T}{m}$
- (D) $\frac{2k_B T}{m}$

Q14. [Marks: 1 | MCQ]

Classical Mechanics · Central Forces

GATE 2012	MCQ	1M
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In a central force field, the trajectory of a particle of mass m and angular momentum L in plane polar coordinates is given by,

$$\frac{1}{r} = \frac{m}{L^2} (1 + \varepsilon \cos\theta)$$

where, ε is the eccentricity of the particle's motion. Which one of the following choices for ε gives rise to a parabolic trajectory?

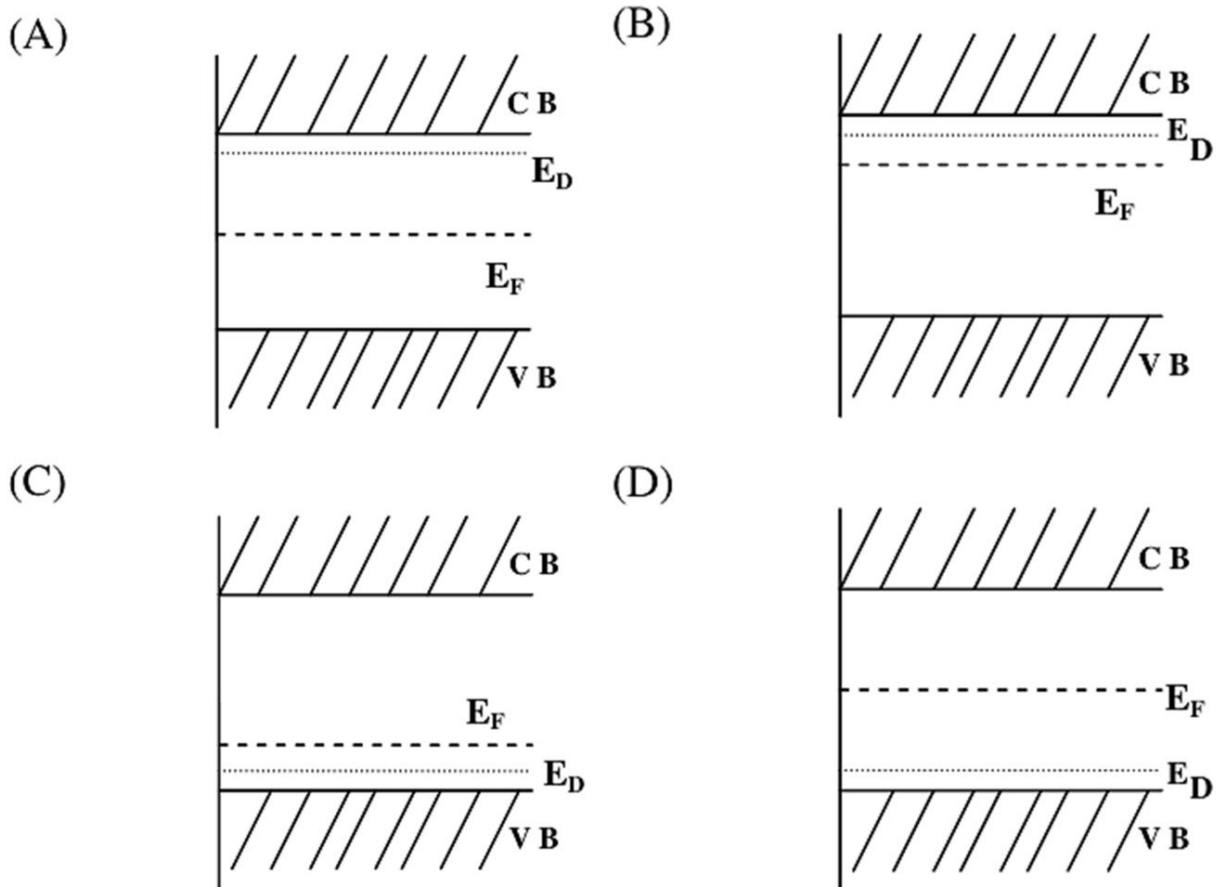
- (A) $\varepsilon = 0$
- (B) $\varepsilon = 1$
- (C) $0 < \varepsilon < 1$
- (D) $\varepsilon > 1$

Q15. [Marks: 1 | MCQ]

Solid State Physics · Semiconductor Physics

GATE 2012	MCQ	1M
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Identify the CORRECT energy band diagram for Silicon doped with Arsenic. Here CB, VB, E_D and E_F are conduction band, valence band, impurity level and Fermi level, respectively.



Q16. [Marks: 1 | MCQ]

Atomic and Molecular Physics · Molecular Physics

GATE 2012	MCQ	1M
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The first Stokes line of a rotational Raman spectrum is observed at 12.96 cm^{-1} . Considering the rigid rotor approximation, the rotational constant is given by

- (A) 6.48 cm^{-1}
- (B) 3.24 cm^{-1}
- (C) 2.16 cm^{-1}
- (D) 1.62 cm^{-1}

Q17. [Marks: 1 | MCQ]

Statistical Mechanics · Quantum Statistical Mechanics

GATE 2012	MCQ	1M
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The total energy, E of an ideal non-relativistic Fermi gas in three dimensions is given by $E \propto \frac{N^{5/3}}{V^{2/3}}$ where N is the number of particles and V is the volume of the gas. Identify the CORRECT equation of state (P being the pressure),

- (A) $PV = \frac{1}{3}E$
- (B) $PV = \frac{2}{3}E$
- (C) $PV = E$
- (D) $PV = \frac{5}{3}E$

Q18. [Marks: 1 | MCQ]

Quantum Mechanics · Spin and Total Angular momentum

GATE 2012	MCQ	1M
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Consider the wavefunction $\Psi = \psi(\vec{r}_1, \vec{r}_2)\chi_s$ for a fermionic system consisting of two spin-half particles. The spatial part of the wavefunction is given by,

$$\psi(\vec{r}_1, \vec{r}_2) = \frac{1}{\sqrt{2}} [\phi_1(\vec{r}_1)\phi_2(\vec{r}_2) + \phi_2(\vec{r}_1)\phi_1(\vec{r}_2)]$$

where ϕ_1 and ϕ_2 are single particle states. The spin part χ_s of the wavefunction with spin states

$\alpha(+1/2)$ and $\beta(-\frac{1}{2})$ should be

(A) $\frac{1}{\sqrt{2}} (\alpha\beta + \beta\alpha)$

(B) $\frac{1}{\sqrt{2}} (\alpha\beta - \beta\alpha)$

(C) $\alpha\alpha$

(D) $\beta\beta$

Q19. [Marks: 1 | MCQ]

Electromagnetism · Potential formulation

GATE 2012	MCQ	1M
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The electric and the magnetic fields $\vec{E}(z, t)$ and $\vec{B}(z, t)$, respectively corresponding to the scalar potential $\phi(z, t) = 0$ and vector potential

$$\vec{A}(z, t) = \hat{i}tz \text{ are}$$

- (A) $\vec{E} = \hat{i}z$ and $\vec{B} = -jt$
- (B) $\vec{E} = \hat{i}z$ and $\vec{B} = jt$
- (C) $\vec{E} = -\hat{i}z$ and $\vec{B} = -jt$
- (D) $\vec{E} = -\hat{i}z$ and $\vec{B} = jt$

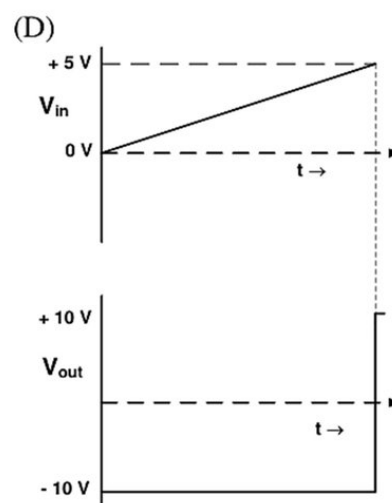
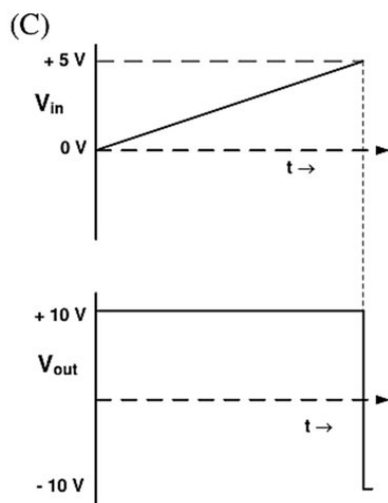
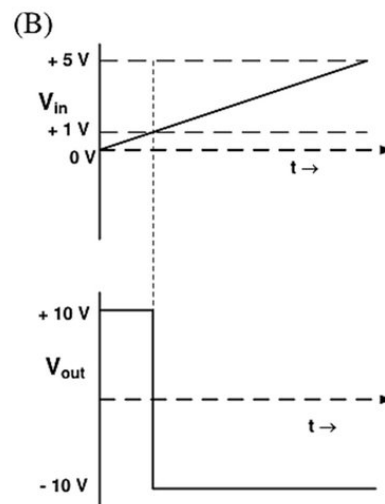
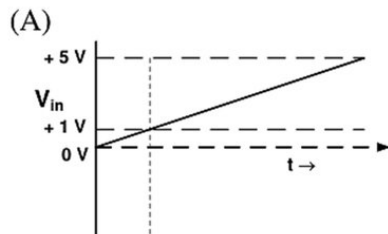
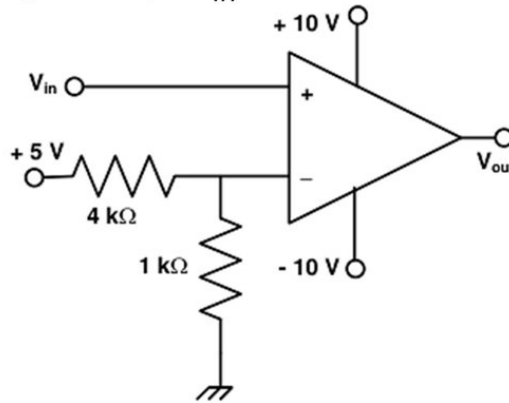
Q20. [Marks: 1 | MCQ]

Electronics · OPAMP

GATE 2012	MCQ	1M
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Consider the following OP-AMP circuit.

Which one of the following correctly represents the output V_{out} corresponding to the input V_{in} ?



Q21. [Marks: 1 | MCQ]

Nuclear and Particle Physics · Nuclear Force, deuteron problem and scatteri

GATE 2012	MCQ	1M
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Deuteron has only one bound state with spin parity 1^+ , isospin 0 and electric quadrupole moment 0.286efm^2 . These data suggest that the nuclear forces are having

- (A) only spin and isospin dependence
- (B) no spin dependence and no tensor components
- (C) spin dependence but no tensor components
- (D) spin dependence along with tensor components

Q22. [Marks: 1 | MCQ]

Classical Mechanics · Small Oscillations

GATE 2012	MCQ	1M
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A particle of unit mass moves along the x -axis under the influence of a potential,

$V(x) = x(x - 2)^2$. The particle is found to be in stable equilibrium at the point $x = 2$. The time period of oscillation of the particle is

- (A) $\frac{\pi}{2}$
- (B) π
- (C) $\frac{3\pi}{2}$
- (D) 2π

Q23. [Marks: 1 | MCQ]

Solid State Physics · Lattice vibration

GATE 2012	MCQ	1M
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Which one of the following CANNOT be explained by considering a harmonic approximation for the lattice vibrations in solids?

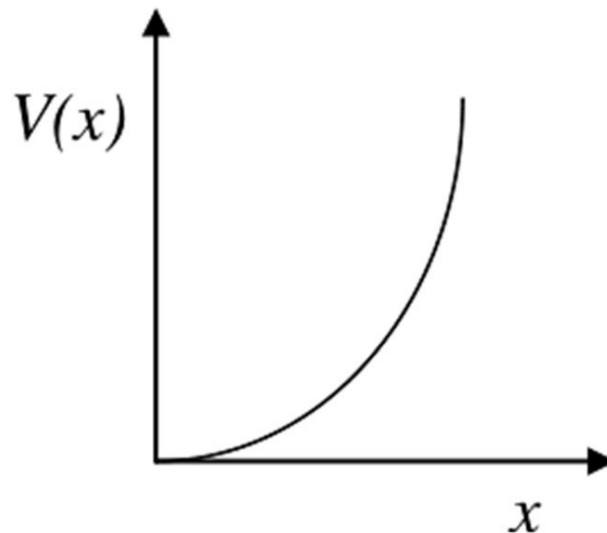
- (A) Debye's T^3 law
- (B) Dulong Petit's law
- (C) Optical branches in lattices
- (D) Thermal expansion

Q24. [Marks: 1 | MCQ]

Quantum Mechanics · Quantum Harmonic Oscillator

GATE 2012	MCQ	1M
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A particle is constrained to move in a truncated harmonic potential well ($x > 0$) as shown in the figure.



Which one of the following statements is CORRECT?

- (A) The parity of the first excited state is even
- (B) The parity of the ground state is even
- (C) The ground state energy is $\frac{1}{2} \hbar \omega$
- (D) The first excited state energy is $\frac{7}{2} \hbar \omega$

Q25. [Marks: 1 | MCQ]

Mathematical Physics · Tensors

GATE 2012	MCQ	1M
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The number of independent components of the symmetric tensor A_{ij} with indices $i, j = 1, 2, 3$ is

- (A) 1
- (B) 3
- (C) 6
- (D) 9

Q26. [Marks: 2 | MCQ]

Quantum Mechanics · Perturbation Theory

GATE 2012	MCQ	2M
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Consider a system in the unperturbed state

described by the Hamiltonian, $H_0 = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$. The

system is subjected to a perturbation of the form

$H' = \begin{pmatrix} \delta & \delta \\ \delta & \delta \end{pmatrix}$, where $\delta \ll 1$. The energy eigenvalues

of the perturbed system using the first order perturbation approximation are

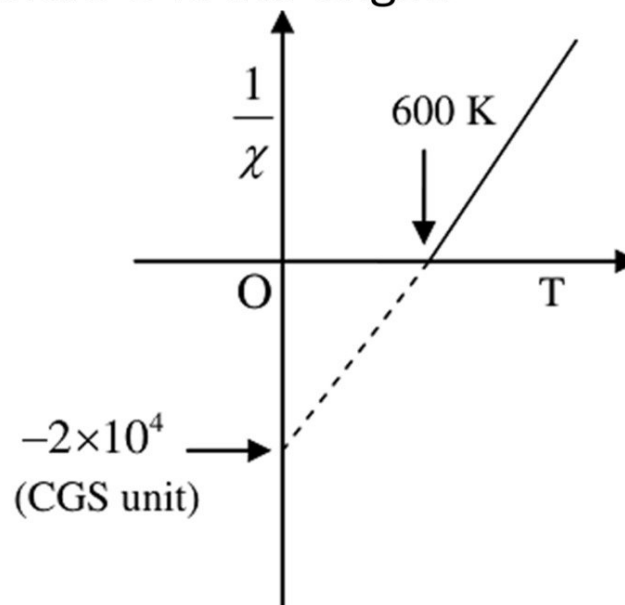
- (A) 1 and $(1 + 2\delta)$
- (B) $(1 + \delta)$ and $(1 - \delta)$
- (C) $(1 + 2\delta)$ and $(1 - 2\delta)$
- (D) $(1 + \delta)$ and $(1 - 2\delta)$

Q27. [Marks: 2 | MCQ]

Solid State Physics · Magnetic properties of solids

GATE 2012	MCQ	2M
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Inverse susceptibility ($1/\chi$) as a function of temperature, T for a material undergoing paramagnetic to ferromagnetic transition is given in the figure, where O is the origin.



The values of the Curie constant, C , and the Weiss molecular field constant, λ , in CGS units, are

- (A) $C = 5 \times 10^{-5}, \lambda = 3 \times 10^{-2}$
- (B) $C = 3 \times 10^{-2}, \lambda = 5 \times 10^{-5}$
- (C) $C = 3 \times 10^{-2}, \lambda = 2 \times 10^4$
- (D) $C = 2 \times 10^4, \lambda = 3 \times 10^{-2}$

Q28. [Marks: 2 | MCQ]

Electromagnetism · EM Waves

GATE 2012	MCQ	2M
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A plane polarized electromagnetic wave in free space at time $t = 0$ is given by

$\vec{E}(x, z) = 10j \exp[i(6x + 8z)]$. The magnetic field $\vec{B}(x, z, t)$ is given by

- (A) $\vec{B}(x, z, t) = \frac{1}{c} (6k - 8\hat{i}) \exp[i(6x + 8z - 10ct)]$
 (B) $\vec{B}(x, z, t) = \frac{1}{c} (6k + 8\hat{i}) \exp[i(6x + 8z - 10ct)]$
 (C) $\vec{B}(x, z, t) = \frac{1}{c} (6k - 8\hat{i}) \exp[i(6x + 8z - ct)]$
 (D) $\vec{B}(x, z, t) = \frac{1}{c} (6k + 8\hat{i}) \exp[i(6x + 8z + ct)]$

Q29. [Marks: 2 | MCQ]

Mathematical Physics · Matrices

GATE 2012	MCQ	2M
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The eigenvalues of the matrix $\begin{pmatrix} 0 & 1 & 0 \\ 1 & 0 & 1 \\ 0 & 1 & 0 \end{pmatrix}$ are

- (A) 0, 1, 1
 (B) $0, -\sqrt{2}, \sqrt{2}$
 (C) $\frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}}, 0$
 (D) $\sqrt{2}, \sqrt{2}, 0$

Q30. [Marks: 2 | MCQ]

Electromagnetism · EM Waves

GATE 2012	MCQ	2M
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Match the typical spectroscopic regions specified in Group I with the corresponding type of transitions in Group II.

Group I

- (P) Infra-red region
- (Q) Ultraviolet-visible region
- (R) X-ray region
- (S) γ -ray region

Group II

- (i) electronic transitions involving valence electrons
- (ii) nuclear transitions
- (iii) vibrational transitions of molecules
- (iv) transitions involving inner shell electrons

- (A) (P, i); (Q, iii); (R, ii); (S, iv)
- (B) (P, ii); (Q, iv); (R, i); (S, iii)
- (C) (P, iii); (Q, i); (R, iv); (S, ii)
- (D) (P, iv); (Q, i); (R, ii); (S, iii)

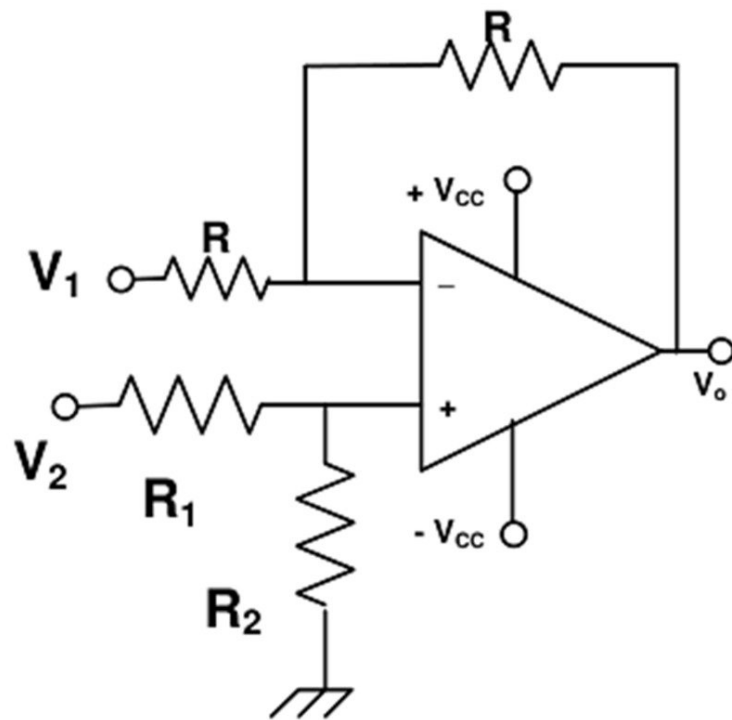
Q31. [Marks: 2 | MCQ]

Electronics · OPAMP

GATE 2012	MCQ	2M
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In the following circuit, for the output voltage to be $V_o = (-V_1 + V_2/2)$, the ratio R_1/R_2 is

- (A) $1/2$
- (B) 1
- (C) 2
- (D) 3



Q32. [Marks: 2 | MCQ]

Quantum Mechanics · Spin and Total Angular momentum

GATE 2012	MCQ	2M
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The terms $\{j_1, j_2\}_J$ arising from $2s^1 3d^1$ electronic configuration in $j - j$ coupling scheme are

- (A) $\left\{\frac{1}{2}, \frac{3}{2}\right\}_{2,1}$ and $\left\{\frac{1}{2}, \frac{5}{2}\right\}_{3,2}$
- (B) $\left\{\frac{1}{2}, \frac{1}{2}\right\}_{1,0}$ and $\left\{\frac{1}{2}, \frac{3}{2}\right\}_{2,1}$
- (C) $\left\{\frac{1}{2}, \frac{1}{2}\right\}_{1,0}$ and $\left\{\frac{1}{2}, \frac{5}{2}\right\}_{3,2}$
- (D) $\left\{\frac{3}{2}, \frac{1}{2}\right\}_{2,1}$ and $\left\{\frac{1}{2}, \frac{5}{2}\right\}_{3,2}$

Q33. [Marks: 2 | MCQ]

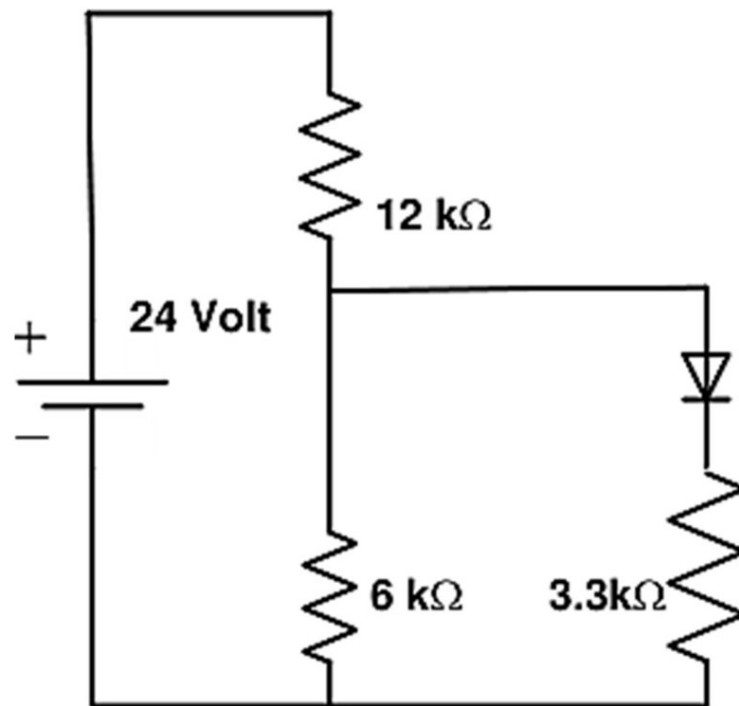
Electronics · Diodes

GATE 2012

MCQ

2M

In the following circuit, the voltage drop across the ideal diode in forward bias condition is 0.7 V .



The current passing through the diode is

- (A) 0.5 mA
- (B) 1.0 mA
- (C) 1.5 mA
- (D) 2.0 mA

Q34. [Marks: 2 | MCQ]

Nuclear and Particle Physics · Particle Physics

GATE 2012	MCQ	2M
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Choose the CORRECT statement from the following.

- (A) Neutron interacts through electromagnetic interaction
 - (B) Electron does not interact through weak interaction
 - (C) Neutrino interacts through weak and electromagnetic interaction
 - (D) Quark interacts through strong interaction but not through weak interaction
-

Q35. [Marks: 2 | MCQ]

Classical Mechanics · Special theory of relativity

GATE 2012	MCQ	2M
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A rod of proper length l_0 oriented parallel to the x -axis moves with speed $2c/3$ along the x -axis in the S -frame, where c is the speed of the light in free space. The observer is also moving along the x -axis with speed $c/2$ with respect to the S -frame. The length of the rod as measured by the observer is

- (A) $0.35l_0$
- (B) $0.48l_0$
- (C) $0.87l_0$
- (D) $0.97l_0$

Q36. [Marks: 2 | MCQ]

Solid State Physics · Crystallography

GATE 2012	MCQ	2M
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A simple cubic crystal with lattice parameter a_c undergoes transition into a tetragonal structure with lattice parameters $a_t = b_t = \sqrt{2}a_c$ and $c_t = 2a_c$, below a certain temperature. The ratio of the interplanar spacings of $(1\ 0\ 1)$ planes for the cubic and the tetragonal structures is

(A) $\sqrt{\frac{1}{6}}$

(B) $\frac{1}{6}$

(C) $\sqrt{\frac{3}{8}}$

(D) $\frac{3}{8}$

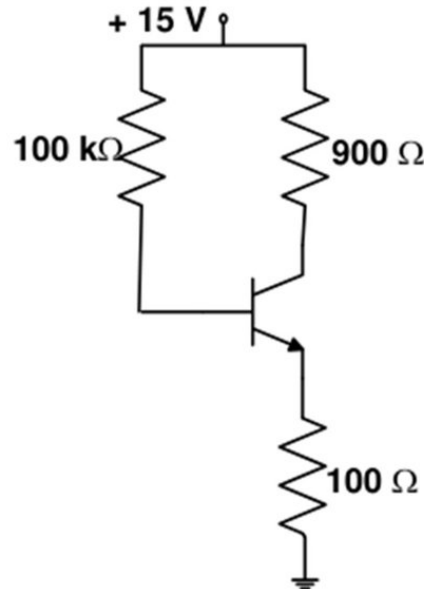
Q37. [Marks: 2 | MCQ]

Electronics · Transistors

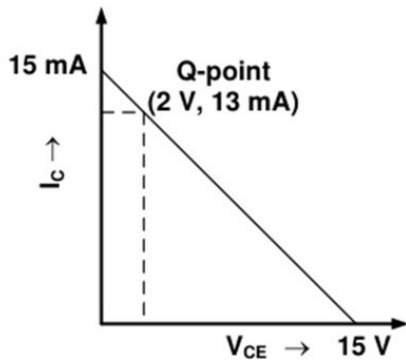
GATE 2012	MCQ	2M
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Consider the following circuit in which the current gain β_{dc} of the transistor is 100 .

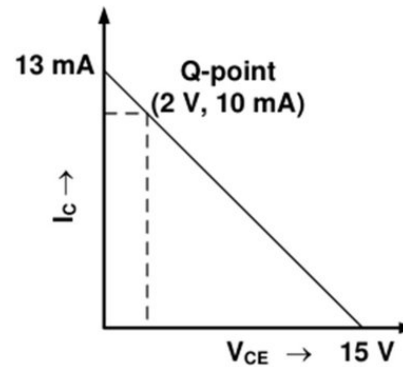
Which one of the following correctly represents the load line (collector current I_C with respect to collector-emitter voltage V_{CE}) and Q-point of this circuit?



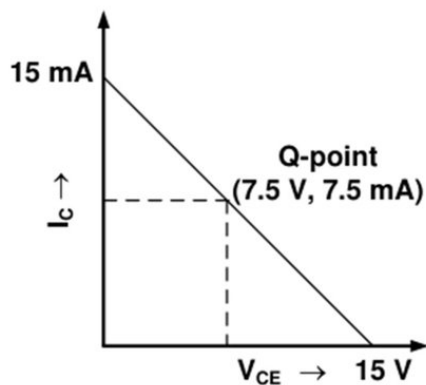
(A)



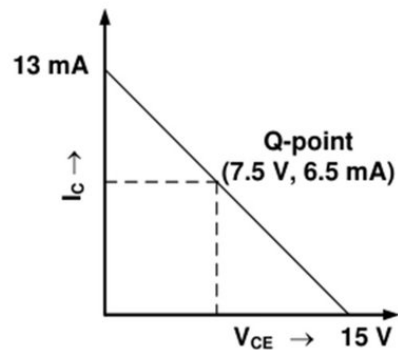
(B)



(C)



(D)



Q38. [Marks: 2 | MCQ]

Statistical Mechanics · Canonical ensemble

GATE 2012	MCQ	2M
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Consider a system whose three energy levels are given by 0 , ε and 2ε . The energy level ε is two-fold degenerate and the other two are non-degenerate.

The partition function of the system with $\beta = \frac{1}{k_B T}$ is given by

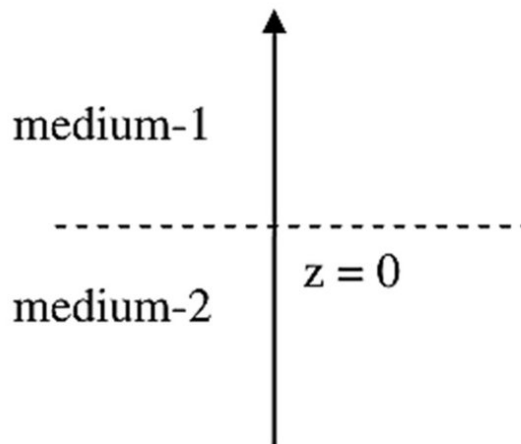
- (A) $1 + 2e^{-\beta\varepsilon}$
- (B) $2e^{-\beta\varepsilon} + e^{-2\beta\varepsilon}$
- (C) $(1 + e^{-\beta\varepsilon})^2$
- (D) $1 + e^{-\beta\varepsilon} + e^{-2\beta\varepsilon}$

Q39. [Marks: 2 | MCQ]

Electromagnetism · Electric field in matter

GATE 2012	MCQ	2M
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Two infinitely extended homogeneous isotropic dielectric media (medium-1 and medium-2 with dielectric constants $\frac{\epsilon_1}{\epsilon_0} = 2$ and $\frac{\epsilon_2}{\epsilon_0} = 5$, respectively) meet at the $z = 0$ plane as shown in the figure. A uniform electric field exists everywhere.



For $z \geq 0$, the electric field is given by

$\vec{E}_1 = 2\hat{i} - 3\hat{j} + 5\hat{k}$. The interface separating the two media is charge free.

The electric displacement vector in the medium- 2 is given by

(A) $\vec{D}_2 = \epsilon_0[10\hat{i} + 15\hat{j} + 10\hat{k}]$

(B) $\vec{D}_2 = \epsilon_0[10\hat{i} - 15\hat{j} + 10\hat{k}]$

(C) $\vec{D}_2 = \epsilon_0[4\hat{i} - 6\hat{j} + 10\hat{k}]$

(D) $\vec{D}_2 = \epsilon_0[4\hat{i} + 6\hat{j} + 10\hat{k}]$

Q40. [Marks: 2 | MCQ]

Quantum Mechanics · Orbital angular momentum and hydrogen atom

GATE 2012

MCQ

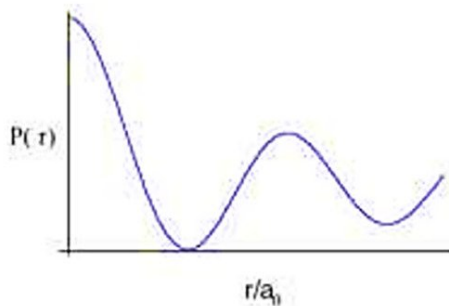
2M

The ground state wavefunction for the hydrogen

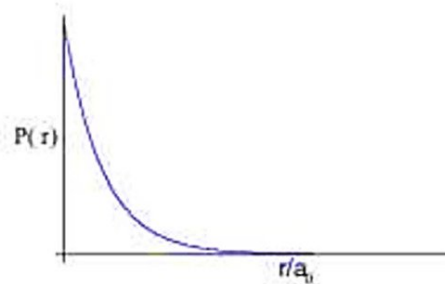
atom is given by $\psi_{100} = \frac{1}{\sqrt{4\pi}} \left(\frac{1}{a_0}\right)^{3/2} e^{-r/a_0}$, where a_0 is the Bohr radius.

The plot of the radial probability density, $P(r)$ for the hydrogen atom in the ground state is

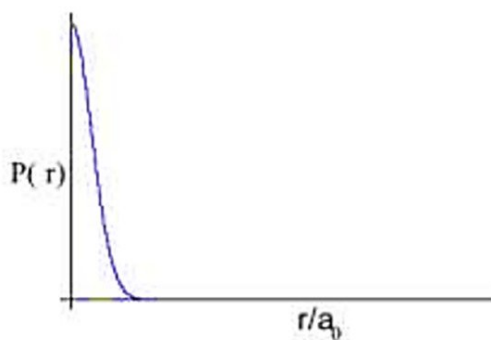
(A)



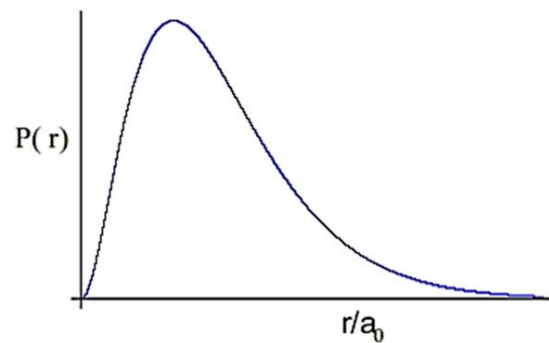
(B)



(C)



(D)



Q41. [Marks: 2 | MCQ]

Nuclear and Particle Physics · Shell Model

GATE 2012	MCQ	2M
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Total binding energies of O^{15} , O^{16} and O^{17} are 111.96 MeV, 127.62 MeV and 131.76 MeV, respectively. The energy gap between $1p_{1/2}$ and $1d_{5/2}$ neutron shells for the nuclei whose mass number is close to 16, is

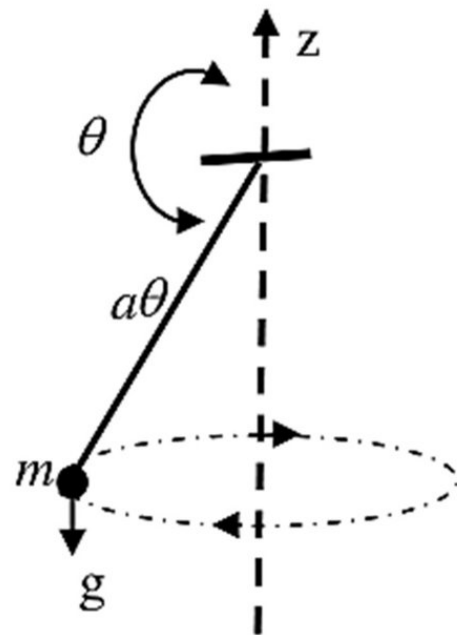
- (A) 4.1 MeV
- (B) 11.5 MeV
- (C) 15.7 MeV
- (D) 19.8 MeV

Q42. [Marks: 2 | MCQ]

Classical Mechanics · Lagrangian and Hamiltonian

GATE 2012	MCQ	2M
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A particle of mass m is attached to a fixed point O by a weightless inextensible string of length a . It is rotating under the gravity as shown in the figure.



The Lagrangian of the particle is

$$L(\theta, \phi) = \frac{1}{2} ma^2 (\dot{\theta}^2 + \sin^2 \theta \dot{\phi}^2) - mg a \cos \theta$$

where θ and ϕ are the polar angles.

The Hamiltonian of the particle is

$$(A) H = \frac{1}{2ma^2} \left(p_\theta^2 + \frac{p_\phi^2}{\sin^2 \theta} \right) - mg a \cos \theta$$

$$(B) H = \frac{1}{2ma^2} \left(p_\theta^2 + \frac{p_\phi^2}{\sin^2 \theta} \right) + mg a \cos \theta$$

$$(C) H = \frac{1}{2ma^2} (p_\theta^2 + p_\phi^2) - mg a \cos \theta$$

$$(D) H = \frac{1}{2ma^2} (p_\theta^2 + p_\phi^2) + mg a \cos \theta$$

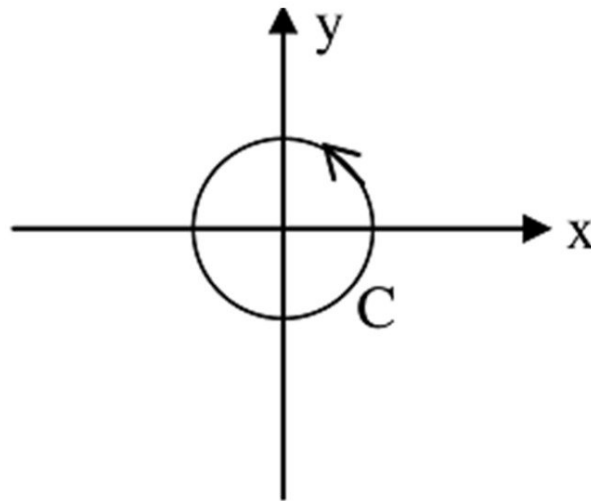
Q43. [Marks: 2 | MCQ]

Mathematical Physics · Vector Analysis

GATE 2012	MCQ	2M
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Given $\vec{F} = \vec{r} \times \vec{B}$, where $\vec{B} = B_0(\hat{i} + \hat{j} + \hat{k})$ is a constant vector and \vec{r} is the position vector. The value of $\oint_C \vec{F} \cdot d\vec{r}$, where C is a circle of unit radius centered at origin is,

- (A) 0
 (B) $2\pi B_0$
 (C) $-2\pi B_0$
 (D) 1



Q44. [Marks: 2 | MCQ]

Mathematical Physics · Complex Analysis

GATE 2012	MCQ	2M
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The value of the integral $\oint_C e^{1/z} dz$, using the contour C of circle with unit radius $|z| = 1$ is

- (A) 0
 (B) $1 - 2\pi i$
 (C) $1 + 2\pi i$
 (D) $2\pi i$

Q45. [Marks: 2 | MCQ]

Statistical Mechanics · Microstates

GATE 2012	MCQ	2M
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A paramagnetic system consisting of N spin-half particles, is placed in an external magnetic field. It is found that $N/2$ spins are aligned parallel and the remaining $N/2$ spins are aligned antiparallel to the magnetic field. The statistical entropy of the system is,

- (A) $2Nk_B \ln 2$
- (B) $\frac{N}{2} k_B \ln 2$
- (C) $\frac{3N}{2} k_B \ln 2$
- (D) $Nk_B \ln 2$

Q46. [Marks: 2 | MCQ]

Atomic and Molecular Physics · Molecular Physics

GATE 2012	MCQ	2M
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The equilibrium vibration frequency for an oscillator is observed at 2990 cm^{-1} . The ratio of the frequencies corresponding to the first and the fundamental spectral lines is 1.96. Considering the oscillator to be anharmonic, the anharmonicity constant is

- (A) 0.005
- (B) 0.02
- (C) 0.05
- (D) 0.1

Q47. [Marks: 2 | MCQ]

Thermodynamics · Kinetic theory of gases

GATE 2012	MCQ	2M
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At a certain temperature T , the average speed of nitrogen molecules in air is found to be 400 m/s.

The most probable and the root mean square speeds of the molecules are, respectively,

- (A) 355 m/s, 434 m/s
- (B) 820 m/s, 917 m/s
- (C) 152 m/s, 301 m/s
- (D) 422 m/s, 600 m/s

Q48. [Marks: 2 | MCQ]

Quantum Mechanics · Basics Quantum Mechanics

GATE 2012	MCQ	2M
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The wavefunction of a particle moving in free space

is given by, $\psi = e^{ikx} + 2e^{-ikx}$

The energy of the particle is

- (A) $\frac{5\hbar^2 k^2}{2m}$
- (B) $\frac{3\hbar^2 k^2}{4m}$
- (C) $\frac{\hbar^2 k^2}{2m}$
- (D) $\frac{\hbar^2 k^2}{m}$

Q49. [Marks: 2 | MCQ]

Quantum Mechanics · Basics Quantum Mechanics

GATE 2012	MCQ	2M
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The wavefunction of a particle moving in free space is given by, $\psi = e^{ikx} + 2e^{-ikx}$

The probability current density for the real part of the wavefunction is

- (A) 1
- (B) $\frac{\hbar k}{m}$
- (C) $\frac{\hbar k}{2m}$
- (D) 0

Q50. [Marks: 2 | MCQ]

Solid State Physics · Tight binding model

GATE 2012	MCQ	2M
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The dispersion relation for a one dimensional monatomic crystal with lattice spacing a , which interacts via nearest neighbour harmonic potential is given by

$$\omega = A \left| \sin \frac{Ka}{2} \right|,$$

where A is a constant of appropriate unit.

The group velocity at the boundary of the first Brillouin zone is

(A) 0

(B) 1

(C) $\sqrt{\frac{Aa^2}{2}}$

(D) $\frac{1}{2} \sqrt{\frac{Aa^2}{2}}$

Q51. [Marks: 2 | MCQ]

Solid State Physics · Tight binding model

GATE 2012	MCQ	2M
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The dispersion relation for a one dimensional monatomic crystal with lattice spacing a , which interacts via nearest neighbour harmonic potential is given by

$$\omega = A \left| \sin \frac{Ka}{2} \right|,$$

where A is a constant of appropriate unit.

The force constant between the nearest neighbour of the lattice is (M is the mass of the atom)

- (A) $\frac{MA^2}{4}$
- (B) $\frac{MA^2}{2}$
- (C) MA^2
- (D) $2MA^2$

Q52. [Marks: 2 | MCQ]

Electromagnetism · Electric field in matter

GATE 2012	MCQ	2M
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In a hydrogen atom, consider that the electronic charge is uniformly distributed in a spherical volume of radius $a (= 0.5 \times 10^{-10} \text{ m})$ around the proton. The atom is placed in a uniform electric field $E = 30 \times 10^5 \text{ V/m}$. Assume that the spherical distribution of the negative charge remains undistorted under the electric field.

In the equilibrium condition, the separation between the positive and the negative charge centers is

- (A) $8.66 \times 10^{-16} \text{ m}$
- (B) $2.60 \times 10^{-15} \text{ m}$
- (C) $2.60 \times 10^{-16} \text{ m}$
- (D) $8.66 \times 10^{-15} \text{ m}$

Q53. [Marks: 2 | MCQ]

Electromagnetism · Electric field in matter

GATE 2012	MCQ	2M
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In a hydrogen atom, consider that the electronic charge is uniformly distributed in a spherical volume of radius $a (= 0.5 \times 10^{-10} \text{ m})$ around the proton. The atom is placed in a uniform electric field $E = 30 \times 10^5 \text{ V/m}$. Assume that the spherical distribution of the negative charge remains undistorted under the electric field.

The polarizability of the hydrogen atom in unit of $(\text{C}^2 \text{ m/N})$ is

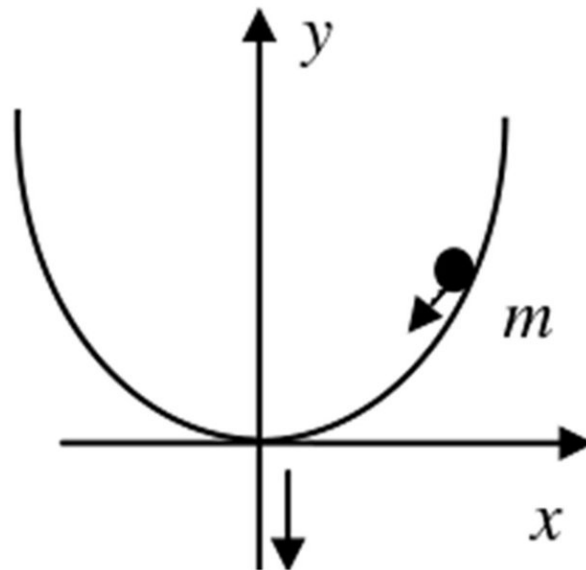
- (A) 2.0×10^{-40}
- (B) 1.4×10^{-41}
- (C) 1.4×10^{-40}
- (D) 2.0×10^{-39}

Q54. [Marks: 2 | MCQ]

Classical Mechanics · Lagrangian and Hamiltonian

GATE 2012	MCQ	2M
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A particle of mass m slides under the gravity without friction along the parabolic path $y = ax^2$ as shown in the figure.



Here a is a constant.

The Lagrangian for this particle is given by,

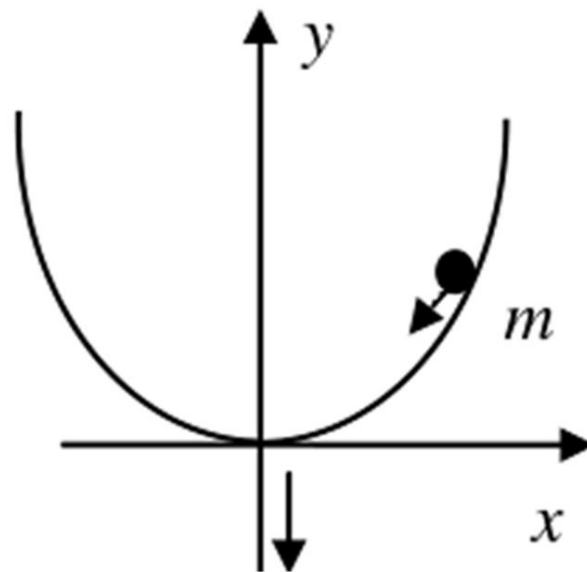
- (A) $L = \frac{1}{2}m\dot{x}^2 - mgax^2$
- (B) $L = \frac{1}{2}m(1 + 4a^2x^2)\dot{x}^2 - mgax^2$
- (C) $L = \frac{1}{2}m\dot{x}^2 + mgax^2$
- (D) $L = \frac{1}{2}m(1 + 4a^2x^2)\dot{x}^2 + mgax^2$

Q55. [Marks: 2 | MCQ]

Classical Mechanics · Lagrangian and Hamiltonian

GATE 2012	MCQ	2M
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A particle of mass m slides under the gravity without friction along the parabolic path $y = ax^2$ as shown in the figure.



Here a is a constant.

The Lagrange's equation of motion of the particle is

- (A) $\ddot{x} = 2gax$
 (B) $m(1 + 4a^2x^2)\ddot{x} = -2mgax - 4ma^2x\dot{x}^2$
 (C) $m(1 + 4a^2x^2)\ddot{x} = 2mgax + 4ma^2x\dot{x}^2$
 (D) $\ddot{x} = -2gax$

Q56. [Marks: 1 | MCQ]

General Aptitude · English

GATE 2012	MCQ	1M
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Choose the grammatically INCORRECT sentence:

- (A) They gave us the money back less the service charges of Three Hundred rupees.
- (B) This country's expenditure is not less than that of Bangladesh.
- (C) The committee initially asked for a funding of Fifty Lakh rupees, but later settled for a lesser sum.
- (D) This country's expenditure on educational reforms is very less.

Q57. [Marks: 1 | MCQ]

General Aptitude · English

GATE 2012	MCQ	1M
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Which one of the following options is the closest in meaning to the word given below?

Mitigate

(A) Diminish

(B) Divulge

(C) Dedicate

(D) Denote

Q58. [Marks: 1 | MCQ]

General Aptitude · English

GATE 2012	MCQ	1M
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Choose the most appropriate alternative from the options given below to complete the following sentence:

Despite several _____ the mission succeeded in its attempt to resolve the conflict.

- (A) attempts
- (B) setbacks
- (C) meetings
- (D) delegations

Q59. [Marks: 1 | MCQ]

General Aptitude · Mathematical Analysis

GATE 2012	MCQ	1M
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The cost function for a product in a firm is given by $5q^2$, where q is the amount of production. The firm can sell the product at a market price of ₹ 50 per unit. The number of units to be produced by the firm such that the profit is maximized is

- (A) 5
- (B) 10
- (C) 15
- (D) 25

Q60. [Marks: 1 | MCQ]

General Aptitude · English

GATE 2012	MCQ	1M
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Choose the most appropriate alternative from the options given below to complete the following sentence:

Suresh's dog is the one _____ was hurt in the stampede.

- (A) that
- (B) which
- (C) who
- (D) whom

Q61. [Marks: 2 | MCQ]

General Aptitude · Reasoning

GATE 2012	MCQ	2M
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Which of the following assertions are CORRECT?

P: Adding 7 to each entry in a list adds 7 to the mean of the list

Q: Adding 7 to each entry in a list adds 7 to the standard deviation of the list

R: Doubling each entry in a list doubles the mean of the list

S: Doubling each entry in a list leaves the standard deviation of the list unchanged

(A) P, Q

(B) Q, R

(C) P, R

(D) R, S

Q62. [Marks: 2 | MCQ]

General Aptitude · Mathematical Analysis

GATE 2012	MCQ	2M
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An automobile plant contracted to buy shock absorbers from two suppliers X and Y. X supplies 60% and Y supplies 40% of the shock absorbers. All shock absorbers are subjected to a quality test. The ones that pass the quality test are considered reliable. Of X's shock absorbers, 96% are reliable. Of Y's shock absorbers, 72% are reliable.

The probability that a randomly chosen shock absorber, which is found to be reliable, is made by Y is

- (A) 0.288
- (B) 0.334
- (C) 0.667
- (D) 0.720

Q63. [Marks: 2 | MCQ]

General Aptitude · Mathematical Analysis

GATE 2012	MCQ	2M
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A political party orders an arch for the entrance to the ground in which the annual convention is being held. The profile of the arch follows the equation $y = 2x - 0.1x^2$ where y is the height of the arch in meters. The maximum possible height of the arch is

- (A) 8 meters
- (B) 10 meters
- (C) 12 meters
- (D) 14 meters

Q64. [Marks: 2 | MCQ]

General Aptitude · Reasoning

GATE 2012	MCQ	2M
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Wanted Temporary, Part-time persons for the post of Field Interviewer to conduct personal interviews to collect and collate economic data.

Requirements: High School-pass, must be available for Day, Evening and Saturday work.

Transportation paid, expenses reimbursed.

Which one of the following is the best inference from the above advertisement?

- (A) Gender-discriminatory
- (B) Xenophobic
- (C) Not designed to make the post attractive
- (D) Not gender-discriminatory

Q65. [Marks: 2 | MCQ]

General Aptitude · Reasoning

GATE 2012	MCQ	2M
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Given the sequence of terms, AD CG FK JP, the next term is

- (A) OV
 - (B) OW
 - (C) PV
 - (D) PW
-

Answer Key

65 questions · Subject & topic for quick revision · Official keys (IIT/IISc)

Q.No	Subject	Topic	Type	Marks	Answer
Q1	Mathematical Physics	Vector Analysis	MCQ	1	A
Q2	Classical Mechanics	Rotation Motion	MCQ	1	C
Q3	Electromagnetism	EM Waves	MCQ	1	A
Q4	Electronics	Diodes	MCQ	1	C
Q5	Quantum Mechanics	Potential Well	MCQ	1	*
Q6	Thermodynamics	Laws of thermodynamics	MCQ	1	A
Q7	Atomic and Molecular Ph...	Effects in atomic physics	MCQ	1	B
Q8	Solid State Physics	Free electron model	MCQ	1	D
Q9	Nuclear and Particle Phy...	Particle Physics	MCQ	1	C
Q10	Nuclear and Particle Phy...	Particle detector and accelerator	MCQ	1	A
Q11	Electromagnetism	EM Waves	MCQ	1	A
Q12	Solid State Physics	Semiconductor Physics	MCQ	1	C
Q13	Thermodynamics	Kinetic theory of gases	MCQ	1	D
Q14	Classical Mechanics	Central Forces	MCQ	1	B
Q15	Solid State Physics	Semiconductor Physics	MCQ	1	*
Q16	Atomic and Molecular Ph...	Molecular Physics	MCQ	1	C
Q17	Statistical Mechanics	Quantum Statistical Mechanics	MCQ	1	B
Q18	Quantum Mechanics	Spin and Total Angular momentum	MCQ	1	B
Q19	Electromagnetism	Potential formulation	MCQ	1	D
Q20	Electronics	OPAMP	MCQ	1	A
Q21	Nuclear and Particle Phy...	Nuclear Force, deuteron problem an...	MCQ	1	D
Q22	Classical Mechanics	Small Oscillations	MCQ	1	B
Q23	Solid State Physics	Lattice vibration	MCQ	1	D
Q24	Quantum Mechanics	Quantum Harmonic Oscillator	MCQ	1	D
Q25	Mathematical Physics	Tensors	MCQ	1	C
Q26	Quantum Mechanics	Perturbation Theory	MCQ	2	A
Q27	Solid State Physics	Magnetic properties of solids	MCQ	2	C
Q28	Electromagnetism	EM Waves	MCQ	2	A
Q29	Mathematical Physics	Matrices	MCQ	2	B
Q30	Electromagnetism	EM Waves	MCQ	2	C
Q31	Electronics	OPAMP	MCQ	2	D
Q32	Quantum Mechanics	Spin and Total Angular momentum	MCQ	2	A
Q33	Electronics	Diodes	MCQ	2	B
Q34	Nuclear and Particle Phy...	Particle Physics	MCQ	2	A
Q35	Classical Mechanics	Special theory of relativity	MCQ	2	D
Q36	Solid State Physics	Crystallography	MCQ	2	C

Answer Key

65 questions · Subject & topic for quick revision · Official keys (IIT/IISc)

Q.No	Subject	Topic	Type	Marks	Answer
Q37	Electronics	Transistors	MCQ	2	A
Q38	Statistical Mechanics	Canonical ensemble	MCQ	2	C
Q39	Electromagnetism	Electric field in matter	MCQ	2	B
Q40	Quantum Mechanics	Orbital angular momentum and hydr...	MCQ	2	D
Q41	Nuclear and Particle Phy...	Shell Model	MCQ	2	B
Q42	Classical Mechanics	Lagrangian and Hamiltonian	MCQ	2	B
Q43	Mathematical Physics	Vector Analysis	MCQ	2	C
Q44	Mathematical Physics	Complex Analysis	MCQ	2	D
Q45	Statistical Mechanics	Microstates	MCQ	2	D
Q46	Atomic and Molecular Ph...	Molecular Physics	MCQ	2	B
Q47	Thermodynamics	Kinetic theory of gases	MCQ	2	A
Q48	Quantum Mechanics	Basics Quantum Mechanics	MCQ	2	C
Q49	Quantum Mechanics	Basics Quantum Mechanics	MCQ	2	D
Q50	Solid State Physics	Tight binding model	MCQ	2	A
Q51	Solid State Physics	Tight binding model	MCQ	2	A
Q52	Electromagnetism	Electric field in matter	MCQ	2	C
Q53	Electromagnetism	Electric field in matter	MCQ	2	B
Q54	Classical Mechanics	Lagrangian and Hamiltonian	MCQ	2	B
Q55	Classical Mechanics	Lagrangian and Hamiltonian	MCQ	2	B
Q56	General Aptitude	English	MCQ	1	D
Q57	General Aptitude	English	MCQ	1	A
Q58	General Aptitude	English	MCQ	1	B
Q59	General Aptitude	Mathematical Analysis	MCQ	1	A
Q60	General Aptitude	English	MCQ	1	*
Q61	General Aptitude	Reasoning	MCQ	2	C
Q62	General Aptitude	Mathematical Analysis	MCQ	2	B
Q63	General Aptitude	Mathematical Analysis	MCQ	2	B
Q64	General Aptitude	Reasoning	MCQ	2	D
Q65	General Aptitude	Reasoning	MCQ	2	A